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Energy Levels of Uranium Ions in Calcium Fluoride Crystals

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The crystal-field-split levels of divalent, trivalent, and tetravalent uranium ions have been studied at 20 °K in selected crystals having single charge-compensation sites. Complete calculations have been made for the free-ion energy levels of \mathbf{U}^{4+} , with the pertinent constants determined as $F_0=13\,175$, $F_2=200$, $F_4=40$, $F_6=8.05$, $\xi_{5f}=1660$, and $\alpha=26$. Also calculated crystal-field-split levels of \mathbf{U}^{4+} in C_{3v} symmetry are compared to experimental values, and the various 'best fit' values of the crystal-field constants determined. ESR results on trigonal $\mathrm{Ca}F_2\colon \mathbf{U}^{4+}$ are correlated with predicted values derived from optical measurements. Experimental studies of the \mathbf{U}^{2+} ion in calcium fluoride are related to the probable \mathbf{U}^{2+} configuration, f^3s . Crystal-field splittings of the lower levels of $\mathrm{Ca}F_2\colon \mathbf{U}^{2+}$ are determined from measurements of absorption and fluorescence at $20^\circ\mathrm{K}$. The calculated value of ξ_{5f} for \mathbf{U}^{2+} , based on approximate L-S coupling conditions for the lowest levels, is $1560~\mathrm{cm}^{-1}$, and is compared with a similarly calculated value for \mathbf{U}^{3+} of $1520~\mathrm{cm}^{-1}$. Experimental crystal-field-split levels of tetragonal $\mathrm{Ca}F_2\colon \mathbf{U}^{3+}$ are shown to fit symmetry requirements, and various laser wavelengths of $\mathrm{Ca}F_2\colon \mathbf{U}^{3+}$ are related to the level system derived from absorption and fluorescence measurements. Temperature shifts of crystal-field-split levels of uranium ions are also reported.

INTRODUCTION

A previous paper¹ presented various aspects of identification and of absorption and fluorescence characteristics of divalent, trivalent, and tetravalent uranium ions influoride crystals. Also, some related papers have been published involving ESR studies of these ions. ²⁻⁶

Further work is reported in the present paper concerning crystal-field-splitting analyses of uranium ions in specific crystal-field sites in calciumfluoride single crystals. Improved spectroscopic facilities have permitted a more adequate presentation of uranium ion energy-level systems than those of the previous paper.

The carefully selected crystal systems covered by this report involve uranium ions of three different valences in essentially single charge-compensation sites. Growth was performed under high vacuum conditions, which permitted the elimination of all oxygen and water contaminations, and in the presence of an adequate supply of F⁻ ions, allowing elimination of residual oxygen and the estab-

lishment of F (not O²⁻) compensation sites. Under these conditions the CaF₂: U²⁺ crystal has a characteristic apple-green color, the CaF₂: U³+ a ruby-red color, and the CaF₂: U⁴⁺ a yellow color. Various other colors which have been observed, such as cerise and shades of brown, involve mixed valence systems or crystals with oxygen contamination. The yellow CaF₂: U⁴⁺ can be readily reduced at room temperature with strong ultraviolet light, gradually converting to a brownish mixture of U3+ and U4+, then to a violet-red crystal of strong U3+ content, and finally to a greenish CaF₂: U²⁺ crystal. This conversion can be monitored by the decrease in absorption in certain sharp infrared absorptions characteristic of U4+, but the reduced ions so produced do not show sharp f to f transitions in the infrared region, apparently as a result of selection rule prohibitions. Complete reconversion of the irradiated crystal is effected by a short heating at 100 °C.

The properties of CaF_2 : U^{5+} , if such a crystal can exist, are unknown. Hexavalent uranium in CaF_2 as a uranyl ion has been prepared in many

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laboratories, including ours. The crystal is colorless, has no free f electrons, and shows strong green uranyl fluorescence to the ground state.

The main components of the instrumentation were a vacuum-type grating spectrometer, ⁷ a lock-in electronic amplifier, ⁸ and a vacuum cryostat, ⁹ which allowed measurements of absorption and fluorescence at crystal temperatures from 20 to 293 °K.

TETRAVALENT URANIUM IONS IN CaF₂

Spectroscopic studies in the infrared, visible, and ultraviolet regions have revealed the crystal-field-split energy-level system of the $5f^2$ electrons of tetravalent uranium ions in C_{3v} symmetry sites in calcium fluoride. Well-delineated sharp levels, characteristic of those required by the crystal symmetry, are evident with almost complete freedom from extra lines of vibrational or other origin that have any appreciable intensity relative to the intensities of the electronic levels. The crystal-field-splittings range from two to five times greater than those for \Pr^{3*} ion in CaF_2 crystals, but are nevertheless in well-defined J-value groupings.

A previous study of uranium ions in calcium fluoride was made by Conway, 10 who showed the general aspects of the solution on a theoretical basis, but without the use of a crystal-field-splitting analysis. Work on tetravalent uranium in various crystal lattices has also been reported by McLaughlin, 11 Richman et al., 12 Satten et al., 13, 14 and others. Except for the Conway study, 10 in which the host crystal was calcium fluoride, these previous studies involved problems of separating vibrational transitions from pure electronic transitions. The differences in the solution presented here from previous solutions result to a considerable extent from the clarification due to the absence of strong vibrational transitions in the trigonal CaF₂: U⁴⁺ crystals.

The 5f² U⁴+ ion is analogous to the 4f² Pr³+ ion, which has been considerably studied in various crystal lattices. Additionally, the isolated free-ion energies of Pr³+ have been experimentally determined by spectroscopic methods, ¹⁵, ¹⁶ and have been fitted to the standard intermediate coupling equations.¹⁵ Deviations of experimental and calculated values of energy levels of these isolated free Pr³+ ions amount to a maximum of about 200 cm⁻¹, even after the introduction of a configuration-interaction correction. But even larger deviations are seen in comparing the experimental isolated free-ion levels of Pr³+ with the corresponding experimentally determined levels in crystals, especially in the higher levels.

The usual method of studying energy levels of ions in crystals involves the experimental determination of the crystal-field-split levels, the identification of them by crystal symmetry properties, and then the calculation of the constants of the pertinent theoretical equations from center-ofgravity (cg) energy values of the levels of each multiplet. The values of the Slater integrals F_0 , F_2 , F_4 , and F_6 , of the spin-orbit interaction ζ , and of the configuration-interaction α , characterize the multiplet system in a particular crystal matrix. Since some levels in the crystal are considerably different from the isolated free-ion values, factors not directly related to the free-ion energy values are dispersed by the calculations into all energies. The fitting depends upon the value of the constants chosen, but usually is the poorest where there is the strongest perturbation by intermediate coupling. For U^{4+} , the spin-orbit coupling constant is considerably larger than for Pr³⁺, with a resultant stronger interplay of energies via the intermediate coupling relationships for the former ion over the latter one.

In view of the factors discussed above, a somewhat different calculation method is employed in the present report from the one commonly used. It does nothing new other than to emphasize the pure R-S multiplets 3F_3 and 3H_5 as primary data for the determination of the solution. These multiplets are only weakly affected by the crystal field (being in the low-energy region) and are readily solved for crystal-field-split levels by high-resolution infrared spectroscopy.

The Slater integrals readily yield the following relationships, which include a Trees configuration-interaction correction, $\alpha L(L+1)$:

$${}^{3}F_{3} - {}^{3}H_{5} = 15F_{2} + 18F_{4} - 273F_{6} - 18\alpha$$
, (1)

$$F_6 = [15F_2 + 18F_4 - (^3F_3 - ^3H_5) - 18\alpha] 1/273, \tag{2}$$

$${}^{3}P_{1} = {}^{3}H_{5} + 14/3 \left({}^{3}F_{3} - {}^{3}H_{5} \right) + 56\alpha ,$$
 (3)

$$\alpha = \left[\left({}^{3}P_{1} - {}^{3}H_{5} \right) - 14/3 \left({}^{3}F_{3} - {}^{3}H_{5} \right) \right] 1/56. \tag{4}$$

Table I contains various experimental data concerning f^2 ions, and illustrates the application of Eqs. (1)-(4), to the solution for various multiplet energies. The solutions for Pr^{3+} served as models for the CaF_2 : U^{4+} calculations of the present report. Knowledge of experimental free-ion values for Pr^{3+} allows appraisal of calculation techniques, whereas true free-ion values for U^{4+} have not been determined.

Optical Spectrum of CaF2: U4+

Figure 1 summarizes the optical-absorption spectrum of trigonally sited U^{4*} ions in calcium-

TABLE I. Free-ion energy levels for f^2 ions.^a

	Free ion Pr ³⁺ Expt ^{b,c}	Free ion Pr ³⁺ Calc ^d	Free ion Pr ³⁺ Calc ^{e, f}	CaF ₂ : Pr ³⁺ tetragonal Expt ^g	CaF ₂ : Pr ³⁺ tetragonal Calc ^{e,h}	CaF ₂ : U ⁴⁺ trigonal Expt ¹	CaF ₂ : U ⁴ * trigonal Calc ^{e, j}
³ H' ₄	0	147	+121	• • •	220	369	930
${}^{3}H_{5}$	2 152	2214	2 152	2256	2 256	5 980	5 980
${}^{3}F_{3}$	6 415	6 2 3 5	6 415	6512	6 512	7 033	7 033
${}^3F_3 - {}^3H_5$	•••	• • •	4263	• • •	4 256	• • •	1 053
${}^{3}P_{1}$	22008	22018	22 046		22 1 26	12352	12357

^a All values are cg energies in cm⁻¹.

 $^{{}^{5}}F_{0}=13175$, $F_{2}=200$, $F_{4}=40$, $F_{6}=8.05$, $\zeta_{f}=1660$, $\alpha=26$, F_{6} from Eq. (2).

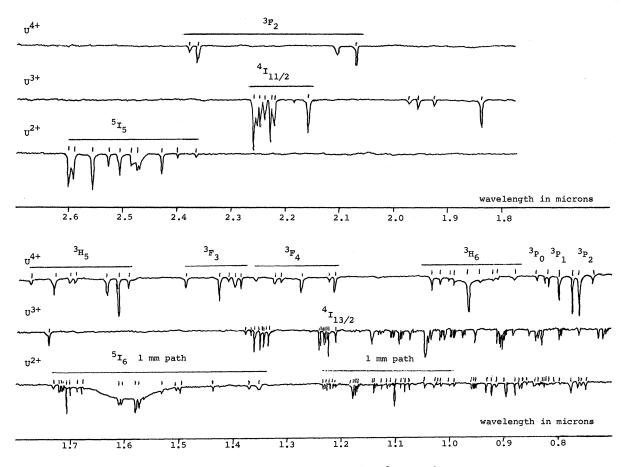


FIG. 1. Crystal-field optical-absorption spectra of U^{4+} , U^{3+} , and U^{2+} ions in CaF_2 at 20 °K.

^bSee Ref. 15.

^eSee Ref. 16.

 $^{{}^{\}text{d}}\text{See Ref.15; } F_0 = 12776, \ F_2 = 322, \ F_4 = 51.6, \ F_6 = 5.14, \ \zeta_f = 741, \ \alpha = 19.$

^{*}Calculations via Eq. (1)-(4) of present paper.

 $^{{}^{}f}F_{0}=13,617, F_{2}=320, F_{4}=59.2, F_{6}=5.87, \zeta_{f}=740, \alpha=0, F_{6} \text{ from Eq. (2)}.$

^gW. A. Hargreaves (unpublished).

 $^{{}^{\}mathbf{h}}F_0 = 13722$, $F_2 = 320$, $F_4 = 59.2$, $F_6 = 5.89$, $\zeta_f = 740$, $\alpha = 0$, F_6 from Eq. (2).

ⁱFrom present paper.

fluoride single crystals at 20 °K. Most of the transitions which appear in Fig. 1 are transitions from a doublet zero ground level to the crystal-fieldsplit levels of the various multiplets. These are identified by a short vertical line adjacent to the maximum absorption position. Some other higher levels of the ${}^{3}H_{4}$ ground multiplet have been identified experimentally by absorption measurements at temperatures higher than the 20 °K temperature involved in the data of Fig. 1. Also, identification of the upper two ${}^{3}H_{4}$ levels was accomplished by optical emission studies at 77 °K. From a 3H_5 level at 6226 cm⁻¹ there is a strong fluorescent transition to a 3H_4 level at 652 cm⁻¹ (wavelength of 1.794 μ), and a weaker transition to a ${}^{3}H_{4}$ level at 1119 cm⁻¹ (wavelength of 1.958 μ). Use is made of this optical-absorption and emission data later in the report when the crystal-field calculations and the free-ion calculations are carried out.

Transition Selection Rules

The nonvanishing crystal-field matrix elements in C_{3v} symmetry are grouped in Hellwege notation as $\mu=0$ and $\mu=\pm 1$ with allowed values of q of 0, ± 3 , and ± 6 . For transition rule purposes, $\mu=0$ can be split into the irreducible representations A_1 and A_2 , and in similar notation the $\mu=\pm 1$ level is an E level. Electric-dipole selection rules derived from Prather¹⁷ show that the allowed transitions are σ for transitions between A_1 or A_2 and E, and π for transitions A_1 to A_1 or A_2 to A_2 . No transitions were seen which did not obey electric-dipole selection rules. The zero energy level of 3H_4 is identified by experiment and calculations as an E level, allowing transitions from it to all upper levels.

Zeeman Studies of CaF_2 : U^{4+}

Optical-absorption Zeeman studies were made at liquid-nitrogen and liquid-helium temperatures, with particular emphasis on the spectral region of the 3P_0 , 3P_1 , and 3P_2 levels. Absorption photographs in σ and π polarization were taken for radiation passing along the 1-cm axis path of a CaF2: U4+ cylinder and dispersed by a 1.8-A/mm spectrometer, with dc magnetic field imposed along a radial [111] trigonal axis. The photographs were studied to identify degenerate levels split by the Zeeman field, and to determine the polarization of the transitions. In C_{3v} symmetry all degenerate levels should show a linear Zeeman effect for magnetic fields parallel to a trigonal axis. El'yashevich¹⁸ gives a good summary of the predicted polarizations for transitions between Zeeman-split levels.

In the plates available, the ${}^{3}H_{4}$ to ${}^{3}P_{0}$ transition

was too weak for Zeeman analysis. In 3P_1 , the absorption 0–12 563 cm⁻¹ was strongly split with the correct σ polarization (being an E to A_2 transition); a transition 123–12 563 cm⁻¹ was too weak for analysis; a 0–12 247 cm⁻¹ (E to E) was correctly π ; and a 79–12 247 cm⁻¹ (A_2 to E) was correctly σ . In 3P_2 , the 0–13 615 cm⁻¹ was too weak to analyze; the 0–13 123 cm⁻¹ (E to E) was correctly π ; and the 0–12 953 cm⁻¹ (E to A_1) was correctly σ . Splittings were evident in other levels (e.g., in 1I_6) but were not analyzed. The fact that all analyzable lines in the 3P manifold show predicted Zeeman characteristics is considered a favorable check on the derived solution.

Contrasting with the Zeeman spectra, no appreciable polarization of CaF_2 : U^{4+} absorption spectra in zero magnetic field is observed in the infrared, visible, or ultraviolet spectral regions. This is true regardless of crystal orientation, and is apparently due to the averaging effects of the four equivalent trigonal axes.

Free-Ion Calculations

Table II compiles the experimental and calculated results of multiplet energies of trigonally

TABLE II. Free-ion levels of U4+.

Multiplet	Expt ^a	Calcb	Composition ^c
	Expt	Care	Composition
${}^{3}H_{4}$	369	930	$91\%^{3}H_{4}$, $8\%^{1}G_{4}$, $1\%^{3}F_{4}$
${}^{3}F_{2}$	4468	3 393	$92\% {}^{3}F_{2}$, $7\% {}^{1}D_{2}$, $1\% {}^{3}P_{2}$
3H_5	5980	5 980	$100\%{}^{3}H_{5}$
${}^{3}F_{3}$	7033	7 033	$100\%{}^3F_3$
3F_4	7 850	8 406	$69\% {}^{3}F_{4}$, $26\% {}^{1}G_{4}$, $5\% {}^{3}H_{4}$
3H_6	10445	10 507	94.7% $^{3}H_{6}$, 5.3% $^{1}I_{6}$
${}^{3}P_{0}$	11 962	10614	97.7% $^{3}P_{0}$, 2.3% $^{1}S_{0}$
${}^{3}\!P_{1}$	12357	12357	$100\%{}^{3}P_{1}$
3P_2	13 286	12549	$82\% {}^{3}P_{2}$, $14\% {}^{1}D_{2}$, $4\% {}^{3}F_{2}$
1G_4	14955	15049	$66\% {}^{1}G_{4}$, $30\% {}^{3}F_{4}$, $4\% {}^{3}H_{4}$
$^{1}I_{6}$	19648	20 087	94.7% $^{1}I_{6}$, 5.3% $^{3}H_{6}$
$^{1}D_{2}$	23 380	$21\ 544$	$78\% {}^{1}D_{2}$, $17\% {}^{3}P_{2}$, $5\% {}^{3}F_{2}$
${}^{1}S_{0}$		47822	

^a The cg energies in cm⁻¹ based on a complete identification of crystal-field-split levels, and a subsequent weighting of singlet and doublet levels, but ${}^{1}I_{6}$ is an average value.

^bCalculated energies in cm⁻¹, with calculation based upon Eqs. (1)-(4) of this paper. The constants are F_0 = 13175, F_2 = 200, F_4 = 40, F_6 = 8.05, ξ_f = 1660, and α = 26.

 $^{^{\}text{c}}\text{Compositions}$ are from eigenvectors of matrix solutions.

sited U^{4*} ions in CaF_2 single crystals. Calculations involve the Slater integrals and the Spedding 19 solutions for f^2 ions in intermediate coupling. All primed multiplets represent intermediate coupling values. The configuration-interaction constant was determined from Eq. (4) of the present paper, using a cg value of 3P_1 based on the experimentally determined crystal-field-split levels. The actual identification of the approximate energy positions of the various levels of the 3P multiplet was based on all aspects of the total solution, including optical absorption and Zeeman data, free-ion calculations, and crystal-field-splitting calculations.

Values of the Slater integrals F_0 , F_2 , and F_4 were determined by trial for a best fit to all levels. The F_6 value was controlled by Eq. (2) of the paper. Since 3H_6 is little affected by intermediate coupling, ξ is fairly well determined by the 3H_6 to 3H_5 interval, and only a small amount of trial fitting was necessary to adequately determine it.

Calculations were performed on a small desk top electronic calculator, using the iterative calculation techniques of Slater, 20 which were adequately handled by the calculator. Final solutions involving matrices greater than 2×2 were rechecked on a large electronic computer.

Crystal-Field Calculations CaF2: U4+

Crystal-field calculations were carried out by means of operator-equivalent methods using the tables of Low, 21 and also by group-theoretical methods using the Eqs. (6-3)-(6-5) of Wybourne, 22 the tabulated data of Nielson and Koster for f^2 electrons, 23 and the 3-j, 6-j symbols of Rotenberg et al. 24 Agreement between the two methods was excellent when a comparison was made using the proportionality constants given by Weber and Bierig. 25 The only discrepancy indicated a required change, to the negative sign, of matrix value 55 of J=6 in Table IX of Low. 21

Tables III and IV compile the crystal-field calculations into summary form, previous to the final calculation of the actual levels. The group-theoretical approach allows the direct calculation of intermediate-coupling matrix multipliers, using the wave function compositions of Table II. For example, the calculation of ${}^{1}G'_{4}$ of ${\rm CaF_2}$: ${\rm U}^{4+}$ involves the linear combination of wave functions:

$${}^{1}G_{4}' = 0.814 \, | \, {}^{1}G_{4} \, \rangle + 0.551 \, | \, {}^{3}F_{4} \, \rangle - 0.186 \, | \, {}^{3}H_{4} \, \rangle$$
. (4)

The intermediate-coupling solution for ${}^{1}G_{4}$ is as follows²⁶:

$${}^{1}G_{4}' = C \begin{pmatrix} JkJ \\ MqM \end{pmatrix} [(0.814)^{2} \langle {}^{1}G_{4} \parallel \mathbf{U}^{k} \parallel {}^{1}G_{4} \rangle$$

$$+(0.551)^{2}\langle {}^{3}F_{4} || U^{k} || {}^{3}F_{4}\rangle + (0.186)^{2}\langle {}^{3}H_{4} || U^{k} || {}^{3}H_{4}\rangle$$

$$-2(0.551) (0.186) \langle {}^{3}H_{4} || U^{k} || {}^{3}F_{4} \rangle].$$
 (5)

The bracketed term in Eq. 5 is a k-dependent value, which, when multiplied by B_q^k , gives the "intermediate-coupling multiplier" of Table IV, column 4.

The final calculated levels of CaF_2 : U^{4*} are listed in Table V, along with the experimentally derived levels. The various B_q^k values listed in Table V are "best fit" values for matching calculated levels to experimental levels.

From Table V we see that the lowest 3H_4 level is a doublet made up of a linear combination of the wave functions involving J_z values of ± 4 , ± 1 , and ± 2 . Since the non-Kramers doublet is involved, spin resonance is only possible through a slight admixture, by way of symmetry distortion, of the wave function of the next higher level.

The value of g_{\perp} is zero, and g_{\parallel} can be expressed in terms of the Landé splitting factor and effective value of J_z , denoted J_z as in

$$g_{II} = 2(0.8) J_e$$
.

From the eigenvectors of the ${}^3H'_4$ solution, given in Table V, the solution calculates as follows:

$$g_{\parallel} = 2. (0.8) (4a^2 + b^2 - 2c^2) = 4.80,$$

with a = 0.817, b = 0.576, and c = 0.015.

The difference of the spectroscopically derived g_{\parallel} from the more direct spin-resonance measurement⁴ of 4.03 lies to some extent in various approximations used in the calculation procedure. It is obvious from the discrepancies between calculated and experimental ${}^3H_4'$ levels (for example) that a perfect calculation has not been accomplished. On the other hand, the correct ${}^3H_4'$ doublet is in the zero-energy position, with close, but not exact, eigenfunction mixing. Also Table V shows a reasonable approximation of all calculated crystal-field-split levels to experimental values. Further refinements in energy interaction calculations might result in improved results.

TRIVALENT URANIUM IN CALCIUM FLUORIDE

Optical-absorption measurements of tetragonally sited U³* ions in calcium fluoride at a temperature of 20 °K have resulted in a modification of the energy-level scheme of the 4I multiplets from the presentation of the previous report. ¹ Two new lines 4452 and 4433 cm⁻¹ appear in the absorption spectrum of $^4I_{11/2}$ at temperatures below about 100 °K. At 20 °K the 4433-cm⁻¹ level becomes the strongest and sharpest of the group. The Kramers doublet levels of the $^4I_{11/2}$ multiplet are now shown in Fig. 2 as six closely spaced levels. They do not include the two more remote lines in the 5000-cm⁻¹

TABLE III. Crystal-field matrix elements in trigonal symmetry.

J	Q	K	J_z 0	±1	± 2	±3	± 4	±5	± 6
1	0	2	-0.3651	+0.1824					
2	0	2	-0.2389	-0.1191	+0.2389				
2	0	4	+0.2389	-0.1593	+0.0398				
			2 -1						
2	3	4	-0.2357						
3	0	2	-0.1952	-0.1464	0	+0.2440			
3	0	4	+0.1612	+0.0268	-0.1880	+0.0806			
3	0	6	-0.1825	+0.1369	-0.0547	+0.0091			
			$2 \ -1$	3 0					
3	3	4	-0.1005	-0.2132					
3	3	6	+0.1774	-0.0836					
			3 -3						
3	6	6	+0.2774						
4	0	2	-0.1699	-0.1444	-0.0679	+0.0594	+0.2378		
4	0	4	+0.1341	+0.0670	-0.0891	-0.1564	+0.1043		
4	0	6	-0.1246	+0.0062	+0.1371	-0.1059	+0.0249		
			$2 \ -1$		3∥0		$4 \parallel +1$		
4	3	4	-0.0623		-0.1564		-0.1649		
4	3	6	+0.0903		+0.1079		-0.1365		
			3∥−3		$4 \parallel - 2$				
4	6	6	+0.1895		+0.1432				
5	0	2	-0.1527	-0.1374	-0.0916	-0.0153	+0.0961	+0.2290	
5	0	4	+0.1183	+0.0788	-0.0197	-0.1183	-0.1183	+0.1183	
5	0	6	-0.1047	-0.0314	+0.0943	+0.0759	-0.1257	+0.0393	
			$2 \ -1$	3 0	$4 \ + 1$	5 2			
5	3	4	-0.0441	-0.1183	-0.1527	-0.1277			
5	3	6	+0.0608	+0.1134	+0.0175	-0.1470			
			3∥−3	$4 \ -2$	5∥ - 1				
5	6	6	+0.1592	+0.1378	+0.0824				
6	0	2	-0.1399	-0.1299	-0.0999	-0.0500	+0.0200	+0.1099	+0.2199
6	0	4	+0.1073	+0.0818	+0.0140	-0.0690	-0.1226	-0.0843	+0.1265
6	0	6	-0.0930	-0.0465	+0.0512	+0.1000	+0.0186	-0.1279	+0.0512
			$2 \ -1$	3 0	4 +1	5∥2	6 3		
	3	4	-0.0334	-0.0929	-0.1309	-0.1359	-0.1009		
6	3	6	+0.0452	+0.1000	+0.0688	-0.0408	-0.1414		
			3 - 3	$4 \parallel -2$	5 -1	6 0			
6	6	6	+0.1414	+0.1291	+0.0957	+0.0512			

region, which were previously thought to be part of this multiplet.

Many fluorescent transitions occur at 20 °K from the $^4I_{11/2}$ crystal-field-split levels to those of $^4I_{9/2}$, and these are also shown in Fig. 2. The first four fluorescent transitions are all CaF₂: U³+ laser transitions. The low-threshold 2.610- μ laser line is more satisfactorily explained with the new $^4I_{11/2}$ level system, as originating from the lowest level of a closely spaced group. The discussion in the previous report¹ of the other fluorescent transitions of tetragonal CaF₂: U³+, and the effect on them of a U²+ impurity in the crystal, is generally correct. When little or no U²+ contamination is present, CaF₂: U³+ at low temperature lases at 2.610 μ , but it lases at 2.565 μ as the crystal tem-

perature approaches room temperature. The 2.510- μ CaF₂: U³⁺ has a high pumping threshold and involves considerable U³⁺ to U²⁺ energy transfer. When the U²⁺content is very high, a ground-state CaF₂: U³⁺ laser of wavelength 2.224 μ can be made to operate at very high pumping power.

In addition to the fluorescent transitions discussed above, several others from much higher levels are reported here. A strong sharp fluorescence of wavelength 4708 Å is the result of a transition from a level at 21842 cm⁻¹ to the ground manifold level at 602 cm⁻¹. Also a weaker fluorescence of 4685 Å is the result of a transition to 497 cm⁻¹ from the same upper level.

Figure 1 shows the infrared portion of the absorption spectrum of tetragonal CaF_2 : U^{3*} at 20 °K.

TABLE IV. Crystal-field matrix multipliers. a

			Intermediate- coupling
Multiplet	k	R-S Multiplier	multiplier
3P_1	2	+0.4008	
${}^{3}F_{3}^{1}$	2	-0.2500	
Ü	4	-0.0555	
	6	+0.2500	
${}^{3}H_{5}$	2	+0.9587	
v	4	-0.6056	
	6	-0.3485	
${}^{3}F_{2}$	2	-0.2332	-0.3003
	4	-0.1177	+0.0465
${}^{3}\!P_{2}$	2	-0.6124	-0.5309
	4	0.0000	-0.1185
$^{1}D_{2}$	2	-0.6414	-0.6515
	4	+0.7062	+0.6522
3H_4	2	+0.9048	+0.8283
	4	-0.6557	-0.7305
	6	-0.6029	-0.3347
${}^3\boldsymbol{F}_4$	2	-0.3419	-0.1084
	4	-0.2575	-0.3953
	6	-0.1220	-0.0554
$^{1}G_{4}$	2	+0.2238	+0.0706
	4	-1.077	-0.8645
	6	+1.198	+0.9367
3H_6	2	+1.109	+1.161
	4	-0.8494	-0.7318
	6	-0.8913	-0.8197
$^{1}I_{6}$	2	+2.219	+2.147
-	4	+1.275	+1.155
	6	+0.3565	+0.2882

^aValues to be multiplied by matrix elements of Table III and by appropriate B_q^k to determine matrix energy values in cm⁻¹.

In connection with the present study, the entire spectrum has been obtained from the longest infrared wavelengths to about 3000 Å in the ultraviolet. The mathematical analysis of these data is a considerable task, and has not been accomplished, but some interesting results are obtained from the lower (infrared) energy levels.

Since all of the 4I multiplets are split in the tetragonal field into Kramers doublets, the cg values of the $^4I_{11/2}$ and $^4I_{9/2}$ can be readily determined as 4500 and 313 cm⁻¹, respectively. If L-S coupling is approximately true for these low levels, the ξ_{5f} value for \mathbb{U}^{3+} computes to be 1520. From this value of ξ_{5f} , an L-S coupling position for $^4I_{13/2}$ is calculated at 9433 cm⁻¹, and similarly for $^4I_{15/2}$ at 15133 cm⁻¹. Inspection of Fig. 1 shows that above the $^4I_{11/2}$ absorption levels at 4500 cm⁻¹ there are some weak lines in the 5100-cm⁻¹ (1.96- μ) region, and two strong sharp lines at 5446 cm⁻¹ (1.836 μ) and 5747 (1.740 μ). These groups do not appear to be connected to the $^4I_{13/2}$ multiplet, which in tetragonal symmetry would consist of seven crystal-

field-split lines. A group of eight lines at 7410-cm⁻¹ cg (1.35- μ region), or a group of seven lines at 8154-cm⁻¹ cg (1.23- μ region), are more likely candidates for ${}^4I_{13/2}$. The lines between ${}^4I_{11/2}$ and ${}^4I_{13/2}$, mentioned

The lines between ${}^4I_{11/2}$ and ${}^4I_{13/2}$, mentioned above, would then be penetrations of the energy region occupied mainly by the 4I multiplets by other multiplets. This is suggested by the energy-level scheme of Fig. 21 of Dieke, 27 which is a survey-type analysis based upon intermediate-coupling calculations for a hydrogenic atom, with estimated field constants. The several weak lines sitting on top of a high transmission band of ${\rm CaF_2}$: ${\rm U}^{3+}$ near 5100 cm $^{-1}$ are about 600 cm $^{-1}$ from the very strong ${}^4I_{11/2}$ levels and may be vibrational in origin.

DIVALENT URANIUM IONS IN CALCIUM FLUORIDE

Evidence showing the existence of divalent uranium ions in calcium-fluoride single crystals was presented in the previous report. The evidence involved studies of the ion as it exists in the unusual physical environment of an impurity site in a crystal. The U^{2*} ion in the CaF_2 crystal is in a stable and permanent condition even at room temperature. However, any attempts to remove it from the crystal to study chemical or other properties would be unsuccessful, since conversion to U^{3*} or U^{4*} ions would be almost spontaneous.

An interesting and rather convincing experiment can be added to the evidence of the previous report to substantiate the U^{2+} ion identification. The green crystals of CaF_2 : U^{2+} can be heated for 2 h in high vacuum, in contact only with platinum, at a temperature of $1100\,^{\circ}$ C, and partially converted to CaF_2 : U^{3+} . The evidence of conversion is an optical-absorption study showing a substantial decrease, following the heat treatment, of the characteristic U^{2+} absorption levels in the 2.5- μ region, and the appearance of definitive U^{3+} 2.15- and 2.22- μ strong absorption lines.

In conjunction with ESR studies which show the ion in question (U²⁺) to be of even valence, further optical studies also confirm the identification.

The U⁴⁺ ion is $5f^2$ and would have 13 possible free-ion energy levels. In a crystal of C_{3v} symmetry, these free-ion levels would be split into 61 levels, and in lowest crystal symmetry would completely split into 91 nondegenerate levels.

A study of the optical-absorption levels of CaF₂: U²⁺ at 20 °K has been made, and 162 sharp absorption transitions from the ground-zero level are evident in the wavelength region from 8 μ in the infrared to 3000 Å in the ultraviolet. There is reason to assume more absorption levels to exist further down in the ultraviolet. The transitions appear in characteristic crystal-field-split groupings, as can be seen in the infrared portion of the spectrum

TABLE V. Crystal-field-splitting levels^a of trigonally sited U⁴⁺ ions in Calcium-Fluoride single crystal at 20 °K. Crystal-field constants are $B_0^2 = -1440$, $B_0^4 = +1000$, $B_0^6 = -1000$, $B_3^4 = \pm 4000$, $B_3^6 = \pm 4130$, and $B_6^6 = \pm 1085$.

Multiplet		Exp	t energ	y and de	egenera	сy			Cal	c ener	gy and	dege	neracy	
3H_4	0 <i>E</i>	$^{79}_{A_2}$			652	1119		$_{E^{\mathfrak{b}}}^{0}$	$^{461}_{A_2}$		1 002 E			
3F_2	$\begin{matrix} 0\\4216\end{matrix}$	$18\\4234$	$620 \\ 4836$					$\begin{matrix} 0 \\ A_1 \end{matrix}$	27 E					
3H_5	0 5 660	$141 \\ 5800$	$241 \\ 5898$	276 5 935	$481 \\ 6140$	$568 \\ 6227$	637 6296	0 <i>E</i>	63 <i>E</i>		$^{460}_{A}$	578 E	$720 \\ A$	794 E
${}^{3}F_{3}$	$\begin{matrix} 0 \\ 6743 \end{matrix}$	289 7 032	$379 \\ 7122$	$435 \\ 7178$	493 7 236			0 <i>E</i>	109 <i>A</i>		410 A	424 E		
3F_4	$\begin{matrix} 0 \\ 7385 \end{matrix}$	196 7 581	$\frac{266}{7651}$	495 7 880	822 8 2 0 7	8 93 8 278		$_{A}^{0}$	4_E		383 <i>A</i>	610 E	648 A	
3H_6	$\begin{matrix} 0 \\ 1173 \end{matrix}$	154 1305	$322 \\ 1720$	511	672	921		$\begin{matrix} 0 \\ 1562 \end{matrix}$	$68\\1630$	365 1 806	939	1 068	1 217	
	$9708 \\ 10881$			10 219	10 380	10 629		$_{E}^{A}$	$egin{array}{c} A \ A \end{array}$	$E \\ A$	E	\boldsymbol{A}	E	
${}^{3}P_{0}$	11962A	1						11 962 <i>A</i>	1					
3P_1	$0\\11247E$		316 12 5634	1_2				0 <i>E</i>	$^{316}_{A_2}$					
3P_2	$0\\12\ 953A_1$	1	170 13 123 <i>1</i>	₹	662 13 615 <i>E</i>	Ē		$\begin{matrix} 0 \\ A_1 \end{matrix}$	230 E	532 <i>E</i>				
1G_4	0 14 267	$240 \\ 14507$	487 14754	652 14 919	$1080 \\ 15347$	1759 16026		0 <i>E</i>	116 <i>A</i>	1 081 E	1 302 A	2 481 E	2 854 A	
¹ D ₂	$0 \\ 22548$	976 23 524	1104 23 652					0 <i>E</i>	571 A ₁	1 312 E				

^a Energy levels in cm⁻¹.

shown in Fig. 1. Such an absorption spectrum of an even-valence ion is only explainable if the ion is U^{2+} of configuration $5f^4$, $5f^3d$, or $5f^3s$.

The $CaF_2: U^{2+}$ was previously assumed as $5f^3d$,

The $\operatorname{CaF_2}\colon \operatorname{U^{2+}}$ was previously assumed as $5f^3d$, with ground state 5L_6 , but evidence now indicates $5f^3s$ as the true configuration. Figure 3 shows the lowest levels of $\operatorname{CaF_2}\colon \operatorname{U^{2+}}$, based on absorption and fluorescence measurements. The approximate average energies of the two lowest multiplets are $4000~\mathrm{cm^{-1}}$ for 5I_5 and $100~\mathrm{cm^{-1}}$ for 5I_4 . Assuming L-S coupling as a rough approximation, we calculate ζ_{5f} as 2(3900/5) or 1560. From Judd, 28 we have the relationships

$$\zeta_{U^{1+}} \approx \zeta_{U^{2+}} \approx \zeta_{U^{3+}}$$
.

The ζ_{5f} value calculated for U^{3*} in the present report is 1520, about the same as that for U^{2*} . A similar calculation using 5L_6 and 5L_7 as the CaF₂: U^{2*} multiplets shows unsatisfactory agreement

The $5f^3d$ configuration would have 386 free-ion levels which would split in a crystal of low symmetry to 3640 nondegenerate levels. For a higher

symmetry there would be considerably less than 3640 levels, but still a large number. The configuration $5f^3s$ has 82 free-ion levels, and 728 levels in a crystal of lowest symmetry. This appears a more likely relationship to the observed 162 crystal-field-split lines found in the covered portion of the optical-absorption spectrum of CaF_2 : U^{2+} .

In trigonal symmetry the 5I_4 level would show 6 crystal-field split lines with 7 lines for 5I_5 and 9 lines for 5I_6 . Table VI lists the levels of ${\rm CaF_2}\colon {\rm U}^{2+}$ in the infrared region as determined from absorption measurements. If these are various 5I multiplet groupings, it is evident that the multiplets exhibit more crystal-field-split lines than called for in trigonal symmetry. A tentative explanation of this is also a tentative explanation for the existence of ${\rm U}^{2+}$ ions in noncubic sites in ${\rm CaF_2}$. Precision density measurements indicate that ${\rm U}^{2+}$ ions in the ${\rm CaF_2}$ lattice are in addition sites, discussed in the previous report. The density of a ${\rm CaF_2}\colon {\rm U}^{2+}$ crystal with a measured ${\rm U}^{2+}$ content is too high to be explained on a substitutional basis. As in the

b One of the states of the lowest ${}^{3}H_{4}$ doublet is 0.817|4>-0.576|1>-0.015|-2>.

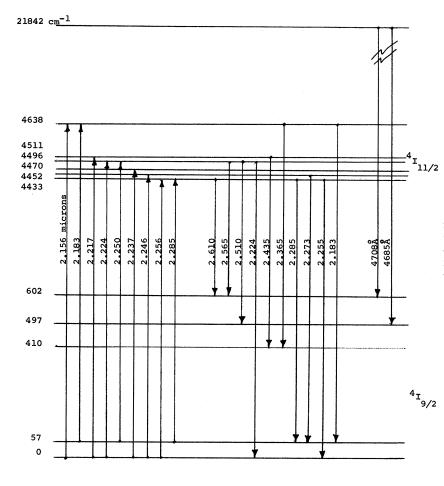


FIG. 2. Optical absorption and fluorescence transitions involving the lower energy levels of tetragonal U³⁺ ions in calcium fluoride at 20 °K. The energy scale breaks between free-ion states.

prebios report, it is postulated that U2+ ions enter normally vacant interstitial sites with two F compensating ions in two nearest, normally empty, interstitial sites having a contiguous edge. The resultant charge compensation is not in a [111] crystal direction as in CaF_2 : U^{4+} , but [112]. This [112] compensation direction would yield lower symmetry than C_{3v} , with a resultant increase in the number of crystal-field-split lines for a given multiplet. In a (110) plane, the ESR spectrum of a [112] site would would appear very much like a [111] site spectrum. The corresponding angles between site axes are complementary in the two cases, and the spectrum of the [111] compensation sites would be shifted 90° (with respect to an [001] crystal direction) from the spectrum of [112] compensation sites.

Much remains to be done in the analysis of CaF_2 : U^{2*} but all of the evidence available seems to show that it is been properly identified, and to some extent characterized by some definite physical properties.

TEMPERATURE SHIFT OF URANIUM-ION ENERGY LEVELS

During the course of the work on energy levels of uranium ions in calcium fluoride it was found that some energy-level positions were affected by crystal temperatures. The effect is of interest in itself, but is also of importance in establishing definitive wavelength and energy values for the levels. Johnson *et al.* ²⁹ have reported on the thermal shifting of Nd³⁺ levels in LaF₃, and they refer to other reports concerning this effect.

Figure 4 shows the thermal shifting of all levels of the 3H_5 multiplet of ${\rm CaF_2}$: ${\rm U}^{4+}$ towards lower energies with increasing temperature. Similar results were found for other multiplets of ${\rm U}^{4+}$, with magnitudes of shift up to two times those occurring in 3H_5 .

Careful measurements on tetragonal CaF₂: U³⁺ showed no evidence of a shift in any of the infrared energy levels within a temperature range from 20

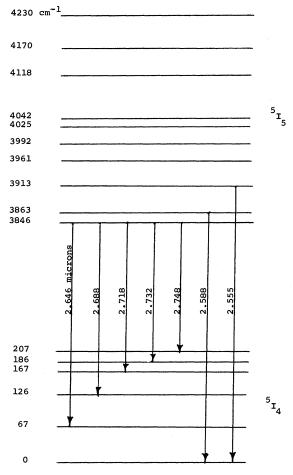


FIG. 3. Optical absorption and fluorescence transitions involving the lower energy levels of U^{2*} ions in calcium fluoride at 20 °K. The energy scale breaks between free-ion states.

to 180 $^{\circ}$ K. Any energy shift exceeding 0.5 cm⁻¹ would be readily detected in the measurement procedure used.

Contrary to CaF₂: U^{4+} , all infrared energy levels of CaF₂: U^{2+} of sufficient sharpness for analysis were found to shift to higher energies with increasing temperature. This is shown in Fig. 4 for the 5I_5 multiplet of U^{2+} . Many other levels in the 1.1- and 1.6- μ regions showed the same order of temperature shift.

DISCUSSION

The identification of U²⁺ ions in crystals is the most controversial subject covered by the author. Spin-resonance results, particular experiments, or calculations are not individually conclusive on this question. The present paper covering analyses of crystal-field spectra supplements the physical and chemical studies of the earlier paper. All of the evidence, when analyzed as a whole, leaves little room for question of the correctness of the identification of the various uranium ions.

ACKNOWLEDGMENTS

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TABLE VI. Infrared energy levels in cm⁻¹ of CaF₂:U^{2*} at 20 °K.

Seven 1	lines of low	oscillator st	rength, with	average er	nergy 10 669	cm ⁻¹ :			
11132	10 965	10 869	10 730	10 504	10 373	10 330			
Sevente	een lines of	high oscillat	or strength,	with avera	ge energy 9	075 cm ⁻¹ :			
10 070	9842	9718	9 5 6 9	9320	9 251	9 200	9099	9009	
8 952	8 88 9	8 780	8 606	8 540	8 511	8 482	8439		
Seven 1	ines of very	low oscilla	tor strength	, with avera	ge energy 8	104 cm ⁻¹ :			
8 347	8 230	8 210	8 1 5 0	8 117	7 936	7740			
Eightee	n lines of v	ery high osc	illator stren	gth, with av	erage energ	gy 6315 cm	1:		
7 418	7315	6 969	6707	6 653	6 540	6 365	6 333	6242	
6215	5 970	5 935	5 886	5 865	5834	5 8 2 7	5 817	5784	
Ten lin	es of low os	cillator stre	ngth, with a	verage ener	gy 4016 cm	ı ⁻¹ :			
$4\ 230$	4170	4118	4042	4 0 2 5	3 992	3 961	3 913	3863	3846
Six line	s with avera	age energy 1	25 cm ⁻¹ :						
207	186	167	126	67	0				

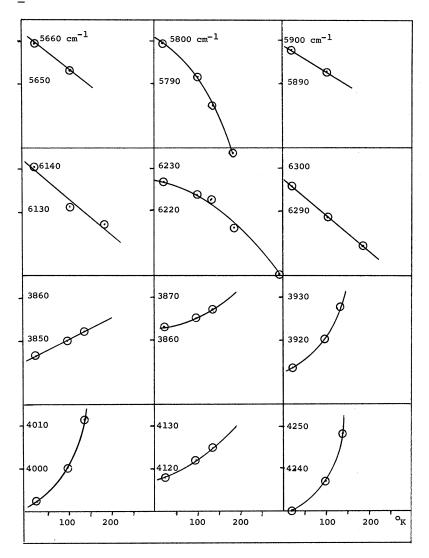


FIG. 4. Temperature shifts of crystal-field-split energy levels in the ³H₅ multiplet of CaF₂: U⁴⁺ (upper six curves), and similarly for the 5I_5 multiplet of CaF2: U2+ (lower six curves). Ordinates of curves are energies of levels in cm⁻¹, and abscissas are temperatures in °K.

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PHYSICAL REVIEW B

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Nuclear Magnetic Resonance in the Cesium-Graphite Intercalation Compounds*

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The C^{13} and Cs^{133} nuclear magnetic resonances have been studied in powdered samples of the cesium-graphite intercalation compounds at temperatures between 1.3 and 4.2 °K. The spin-lattice relaxation times and the line shapes of both nuclear species in the compounds and of the C13 nucleus in pure graphite were measured in an effort to determine the nature of the conduction-electron states in these substances. At 4.2 °K, using pulse techniques, the measured values of T_1 for C^{13} are 1.6 ± 0.3, 2.6 ± 0.4, 3.9 ± 0.5, 5.6 ± 0.5, 7.6 ± 0.8, and 30 ± 5 min in C_8Cs , $C_{24}Cs$, $C_{36}Cs$, $C_{48}Cs$, $C_{60}Cs$, and pure graphite, respectively. Both the Salzano-Aronson binding model for the compounds and a tight-binding extension to the Slonczewski-Weiss band model for graphite are shown to account qualitatively for the cesium concentration dependence of the C^{13} T_1 's. None of the usual relaxation mechanisms is conclusively identified with the relatively short C^{13} T_1 's. The temperature dependence also remains unaccounted for. Echo techniques at helium temperatures establish the shape of the 500-G-wide 16.8 ± 1 kHz. The Knight shift for cesium in C_8Cs is measured to be (0.29 $\pm 0.01\%$), independence dent of temperature from 300 to 1.3 °K. In C24Cs and C36Cs, the Knight shift was zero within $\pm 0.02\%$. The experimentally measured T_1 for Cs¹³³ in C₈Cs was 7.5 ± 0.5 sec, while the T_1 's in $C_{24}Cs$ and $C_{36}Cs$ were 27 ± 6 and 48 ± 10 min, respectively. The Cs^{133} Knight-shift and relaxation-time results support the view that the cesium is partially ionized in C_8Cs and completely ionized in the cesium-poorer stages.

I. INTRODUCTION

The techniques of nuclear magnetic resonance (NMR) have provided detailed information about interactions between nuclei and their environments in a variety of physical systems. This paper reports on the use of these techniques to study one member of an unusual group of crystalline, metallike compounds, the alkali-graphite intercalation compounds.

The crystal structure of these compounds is well known. ¹⁻³ Their static susceptibilities have been measured and are paramagnetic, in contrast to the large diamagnetism of pure graphite. ⁴ Electrical conductivity in the potassium-graphite system increases with increasing alkali concentration, although with different rates in the two different crystal directions. ⁵ Thermodynamic properties, such as energies of formation and alkali vapor pressures, have been measured. ⁶ The most alkali-rich stages of the cesium, rubidium, and potassium compounds have been observed to undergo a superconducting transition. ⁷ The critical field is anisotropic. More recently, an expansion of the carboncarbon bond length with increasing alkali content

has been observed in the potassium-graphite system 8

In general, experimental results are consistent with the assumption that there is a transfer of electronic charge from alkali to the graphite layers. However, little detailed information about the nature of the resulting electronic states is available. The electrostatic binding model of Salzano and Aronson 9, 10 successfully accounts for the bonding energies of all but the two most alkali-rich stages. However this model is not sensitive to the nature of the electronic states.

We report here on the low-temperature magnetic resonance properties of graphite and the cesium-graphite system. The only previous observation of magnetic resonance in these compounds is the work of Jensen, O'Reilly, and Tsang. ¹¹ They observed the cw peak of the Cs¹³³ line in C_8 Cs and C_{24} Cs – a "line" that in this study is shown to be the central peak of a quadrupolar broadened powder pattern. Their quoted values for the cesium Knight shift are in disagreement with results presented here.

Section II is devoted to a brief discussion of the